Simulation of the Nanofiltration of Pulping Black Liquor by Dynamic Blade Cross-flow with Membrane

Wenjie Zhao, Zhongyu Du, Ning Kuang, Hao Wang, Benliang Yu, Junfei Wu,* and Fushan Chen

This paper investigated the filtration of black liquor with blade cross-flow by membrane. The lignin content in black liquid filtered by the nanofiltration membrane (NP010) is high under the transmembrane pressure of 0.5 bar, 1 bar, 1.5 bar, and 2 bar at 300 rpm and 800 rpm. In this regard, the tangential velocity on the nanofiltration membrane surface and the pressure variation on the blade in the process of filtration are simulated and analyzed with Fluent software. The tangential flow velocity on the nanofiltration membrane surface and the dynamic pressure on the blade, as well as the law of change under different rotation speed and transmembrane pressure are obtained. The comparison between experimental and simulated results have validated the numerical model of the filtration of black liquid by the blade dynamic cross-flow. According to the experimental and simulated results, the optimized filtration conditions are obtained when the blade dynamic cross-flow uses 1 kDa nanofiltration membrane to filter black liquor.

Keywords: Dynamic cross-flow; Nanomembrane filtration; Tangential velocity; Dynamic pressure

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INTRODUCTION

Ninety percent of the total waste-water pollutants in the paper-making industry has come from the pulping black liquor. Because the pulping black liquor contains lignin, a biomass difficult to degrade, the treatment of black liquor has become a world-wide problem. Therefore, the treatment of pulping black liquor mainly lies in the proper treatment of lignin. However, lignin is a natural renewable aromatic polymer second only to cellulose. It has good mechanical strength, elasticity, and rheology as well as high carbon content, reactivity, and chemical compatibility. These attributes imply that it also has high application value. Therefore, the recycling of lignin from the pulping black liquor not only can solve the environmental pollution in a fundamental sense, but it can also “turn waste into treasure”.

Membrane filtration technology uses membranes with different cut-off molecular weights to concentrate pulping black liquor to a certain degree, separate lignin with large molecular weight from sugars and organics with small molecular weight, and to obtain pulping black liquor containing lignin with uniform molecular weight distribution and single structure (Wallberg et al. 2003a,b; Wallberg and Jönsson 2006; Ji et al. 2011; Helander et al. 2013; Arkell et al. 2014; Humpert et al. 2016; Al-Rudainy et al. 2017; Durruty 2018; Liu et al. 2018; Hubbe et al. 2019). However, with the passage of time in the process of filtration, the formation of filter cake increases the filtration resistance (De and Bhattacharya 1996; Costa et al. 2018). The biggest feature of dynamic blade cross-flow membrane filtration is that the rotation of the blade causes high shearing stress of the
liquid on the membrane surface, which reduces the filtration resistance caused by the filter cake, thus improving filtration efficiency (Jaffrin 2008; Jönsson et al. 2008; Toledano et al. 2010a,b; Domínguez-Robles et al. 2016, 2018).

Before the simulation of filtering black liquor by blade cross-flow, initial experiments were carried out in which black liquor was filtered by blade cross-flow ultrafiltration (5 kDa, 10 kDa) and nanofiltration (1 kDa). The lignin content was measured in the filtered black liquor. The lignin content was 37% in the nanofiltration experiment and 22% in the ultrafiltration experiment. Experimental research on lignin retention in black liquor based on dynamic blade cross-flow membrane filtration shows that nanofiltration (NP010-1kDa) has a relatively obvious effect on lignin retention in pulping black liquor. According to the theoretical analysis of the average shearing stress on the membrane surface (Bouzerar et al. 2000; Manttari et al. 2015; Kevlich et al. 2017; Ahuja et al. 2018), the average shearing stress shows a non-linear variation with the blade rotation speed (ω) and a linear correlation with the blade radial distance (r) (Jaffrin 2008). Combining theory with experiments, this paper uses the computational fluid dynamics (CFD) software Fluent to perform numerical simulations of lignin retained in pulping black liquor by blade cross-flow. The main purpose of this paper is to investigate the tangential velocity on the membrane surface and the pressure variation on the blade with the radius when the lignin in the black liquor is filtered by the blade cross-flow. These data provide useful information for the application of the blade dynamic cross-flow process to separate the lignin in the black liquor.

**EXPERIMENTAL**

**Materials**

*Experimental equipment*

A DYNO filter provided by BOKELA GmbH (Karlsruhe, Germany) is shown in Fig. 1. The whole process mainly included the control system, data acquisition system, material input system, filtration system, and self-cleaning system. The DYNO filter was composed of rotating blades, filter membranes, stainless steel porous membranes, and other parts. Its basic equipment data are shown in Table 1. The black liquor flowed from vessels into the filter chamber from its inlet through pressure, passed through the polymer membrane and the stainless-steel porous membrane, and finally the filtrate flowed out through the outlet (Bott et al. 2000). Transmembrane pressure (TMP) was controlled by a pressure-measuring valve. The rotor was controlled by a motor and operated at a speed range from 0 rpm to 1000 rpm. The rpm and TMP remained constant during the separation process. The weight of the filtered filtrate was measured by a load sensor, and data such as flux in the filtration process was automatically saved on the computer.

**Table 1. Basic Data of DYNO Filter**

<table>
<thead>
<tr>
<th>Filter Area (m²)</th>
<th>Module Diameter (mm)</th>
<th>Maximum Pressure (bar)</th>
<th>Maximum Temperature (°C)</th>
<th>Velocity (m/s)</th>
<th>Dimensions L × W × H (mm)</th>
<th>Weight (kg)</th>
<th>Drive (kW)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.013</td>
<td>137</td>
<td>6</td>
<td>95</td>
<td>12</td>
<td>639/334/581</td>
<td>48</td>
<td>0.55</td>
</tr>
</tbody>
</table>

The membrane used in the experiment was provided by Microdyn Nadir of Germany, and the detailed data of the membrane is described in Table 2. The black liquor used in the experiment was provided by the Institute of Mechanical Process Engineering and Mechanics of Karlsruher Institut of Technologie, and the basic characteristics of black liquor are shown in Table 3.

**Table 2. Basic Data on Filter Membranes Used in Experimental Studies**

<table>
<thead>
<tr>
<th>Name</th>
<th>Material</th>
<th>Permeability (LMH/bar)</th>
<th>pH range</th>
<th>Standard captured molecular weight (Da)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nanofiltration NP010</td>
<td>PES</td>
<td>≥ 5</td>
<td>0.0–14.0</td>
<td>1,000-1,200</td>
</tr>
<tr>
<td>Ultrafiltration UP005</td>
<td>PES</td>
<td>≥ 10.0</td>
<td>0.0–14.0</td>
<td>5,000</td>
</tr>
<tr>
<td>Ultrafiltration UP010</td>
<td>PES</td>
<td>≥ 50.0</td>
<td>0.0–14.0</td>
<td>10,000</td>
</tr>
</tbody>
</table>
Table 3. Basic Data on Pulping Black Liquor in Experiments

<table>
<thead>
<tr>
<th>Name</th>
<th>Density (kg/m³)</th>
<th>Viscosity (Pa·s)</th>
<th>Lignin content (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pulping black liquor</td>
<td>1098</td>
<td>5.85</td>
<td>9</td>
</tr>
</tbody>
</table>

Experimental Results

The experimental conditions were: 300 rpm, 800 rpm; transmembrane pressure is: 0.5 bar, 1 bar, 1.5 bar, 2 bar; three filtration membranes: UP005, UP010, NP010. The experimental results of the change of lignin content in black liquid are shown in Fig. 2. The lignin content in the black liquor filtered by nanofiltration membrane was higher than other membranes. By comparing the experimental data, it was found that the effect of the nanofiltration membrane (NP010) was ideal for lignin retention and concentration in black liquid. Figure 3 gives the experimental results of the average flux of black liquid filtered by NP010.

Fig. 2. Changes in lignin content in membrane-filtered black liquor (a) 300 rpm; (b) 800 rpm
In the experiment, the nanofiltration membrane (NP010) delivered the best effect on the retention and concentration of lignin in black liquor. Under the operation condition of 300 rpm and 800 rpm, and transmembrane pressures of 0.5 bar, 1 bar, 1.5 bar, and 2 bar, the NP010 retention results are shown in Fig. 3.

![Average flux of black liquor with NP010](image)

**Fig. 3.** Comparison of the average flux of nanofiltration membrane NP010 under different transmembrane pressures and different rotation speed

### ANALOGUE COMPUTATION

#### Theory Basis of Cross-flow Shearing

The magnitude of the membrane flux is related to the transmembrane pressure, the filter cake filtration resistance \(R_m\), and the filtration resistance \(R_c\) of the original membrane, as shown in the basic equation of membrane filtration (Eq. 1). In this regard, how to reduce the filtration resistance of the filter cake is the core issue of increasing the membrane flux. This is shown as Eq. 1,

\[
q_s = \frac{\Delta P}{\mu (R_m + R_c)}
\]

where \(q_s\) represents the flux \((L/(m^2\cdot h))\) of the nanofiltration membrane, \(\Delta P\) represents the pressure \((N/m^2)\), \(\mu\) represents the viscosity \(\text{kg/s} \cdot \text{m})\) of the liquid, \(R_c\) represents the filtration resistance \(\text{m}^{-1}\) of the filter cake, and \(R_m\) represents the filtration resistance \(\text{m}^{-1}\) of the membrane. The formation of filter cake on the membrane surface is prevented by increasing the shearing stress on the membrane surface. According to the research conducted by Bouzerar et al. (2000) on the main characteristics of the internal flow field in this type of system, the local shearing stress exists on the fixed membrane under turbulent and laminar condition.

The local shearing stress for laminar flow:

\[
\tau_{ml} = 0.77 \rho v^{0.5} (\kappa \omega)^{1.5} r
\]

The local shearing stress for turbulent:

\[
\tau_{mt} = 0.0296 \rho v^{0.2} (\kappa \omega)^{1.8} r^{1.6}
\]

In this regard, the shearing stress on the membrane depends on the velocity coefficient \( K, \omega \) (rpm), and the radial distance (m).

**CFD Simulation Settings**

**Geometric modeling**

In the process of the modeling design of the blades and the filter chamber, a geometric three-dimensional graph of the filter chamber was modeled in strict accordance with the size of the blades and the filter chamber in the experimental equipment. The width of the filter chamber was \( T = 137 \) mm, the thickness of the filter chamber was \( H = 30 \) mm, the gap between the blade and the membrane was \( C = 15 \) mm, the diameter of the rotating blade was \( D = 128 \) mm, and the geometric three-dimensional graph of the filter chamber is shown in Fig. 4.

![Fig. 4. Geometric three-dimensional graph of the filter chamber with SolidWorks](image)

**Numerical modeling**

A three-dimensional (3D) model of the filter chamber and rotating blades was modeled in the Unigraphics NX (Siemens PLM Software, 8.5, Plano, TX, USA). Considering that the Markov random field (MRF) model was selected for computation in FLUENT (ANSYS, Inc., 16.0, Canonsburg, PA, USA), the model was partitioned as a whole and the process was completed in the NX. A cylindrical block was created in the filter chamber to enclose the blades as a moving area, while the filter chamber was filled with black liquid as a static area. In addition, a porous medium was established near the outlet of the filter chamber. The methods and steps of constructing the model are shown in Fig. 5.

![Fig. 5. Methods and steps for constructing numerical models](image)
The interior of the blade did not engage in the computation of the flow field and heat transfer was not taken into account. After the 3D model was created, it was imported into Workbench (ANSYS, Inc., 16.0, Canonsburg, PA, USA) for meshing, and the grids of the three areas were refined. A total of 817,211 grids were divided. The generated grids’ quality was reviewed, the average grid quality was 0.82, which indicated quality conformance. The grid model is shown in Fig. 6.

![Grid-based meshing of the overall filter chamber with Workbench](image)

**Fig. 6.** Grid-based meshing of the overall filter chamber with Workbench

*Setting of geometric boundary type*

After the meshing was completed, the initial geometric boundary type of the model was set, that is, the corresponding physical meaning of geometric surface. As shown in Fig. 7, the side ‘In’ is a pressure inlet and ‘Out’ is a pressure outlet; it was correspondingly set as ‘Pressure-Inlet’ and ‘Pressure-Outlet’. The remaining geometric boundary conditions are shown in the figure.

![Settings of geometric boundary type](image)

**Fig. 7.** Settings of geometric boundary type
Conditions for boundary setting

Because the flow field in the chamber is complex, it was assumed that the fluid is constantly incompressible, and the flow process is isothermal. In this paper, the first-level filtering chamber was taken as the research object. The lignin content in black liquor is about 9% consistent with the experiment. The interaction force between the dual-phase liquid and solid was negligible. The shearing stress of the blade on the membrane surface was the research content. As such, single-phase fluid was taken as the flow medium in the chamber for flow field analysis. The radial pulsation of the filtrate after passing through the filter medium was negligible.

To ensure the authenticity and reliability of the numerical simulation of the research objects, each item in setting boundary conditions was directly quoted or indirectly calculated based on the experimental data. The pressure-base implicit solution method was adopted, the k-epsilon RNG under the turbulence model was selected, and the standard wall function was used for near-wall treatment. The physical properties of the fluid include the density (1098 kg/m$^3$) and viscosity (5.85 Pa·s) of the black liquor and the rpm of the rotor was set at 300 rpm and 800 rpm, respectively. The inlet boundaries of the filter chamber were set as pressure inlets, which are 0.5 bar, 1 bar, 1.5 bar, and 2 bar, respectively. The centrifugal force generated by the high-speed rotation of the blade was much greater than gravity, so the effect of gravity was not considered here. The outlet pressure of filtrate was set at 0 bar.

Due to the presence of membranes in the flow field, porous media conditions are required to set the boundary to enhance the calculation accuracy. The momentum equation of the porous medium model is adding the source term to the standard momentum equation, and the source term includes the viscosity loss term and the inertial loss term:

$$S_i = \left( \frac{\mu}{\alpha} v_i + C_2 \frac{1}{2} \rho |v| v_i \right)$$

In the equation: $S_i$ is the source of the momentum equation; $|v|$ is the speed; $\alpha$ is the permeability coefficient, and $C_2$ is the inertial resistance coefficient. That is, the two matrices are simplified to diagonal matrices, with coefficients on the diagonals being $\alpha$ and $C_2$, and elements other than diagonals being 0, and the porous jump parameters including face permeability, porous medium thickness, and pressure coefficient are defined as follows,

$$u = B \frac{\Delta P}{\mu \times L}$$

$$C_2 = \frac{1}{c^2} \frac{[\Delta P/A_p]^2 - 1}{L}$$

where $u$ represents the speed (m/s) of the liquid passing through the filter layer, $B$ represents the permeability (m$^2$) of the filter medium, $L$ represents the filter medium thickness (m), $\Delta P$ represents the transmembrane pressure difference, and $\mu$ represents the viscosity (Pa·s) of black liquor. A high $B$ value means that the liquid is easy to pass through the medium. The smaller the value, the greater the resistance of the medium. In this analysis, $C = 0.98$, representing the porosity of the filter medium.
RESULTS AND DISCUSSION

The simulated results mainly observe the changes in the tangential velocity field on membrane surface and the blade dynamic pressure under different rotation speed and the comparison in flux of experimental and simulated results.

Velocity Field Variation of Nanofiltration Membrane

Due to the shearing action of the blade on the black liquor and the variation in the velocity field on the nanofiltration membrane, the surface is related to the blade rotation rate. The cloud diagrams of the tangential velocity field on the membrane surface at 800 rpm and 300 rpm are shown in Figs. 8 and 9. The variation of tangential velocity with the membrane radius is shown in Figs. 10 and 11. The tangential velocity on the membrane surface gradually increased with the radius. At 300 rpm, the tangential velocity on the membrane gradually increased to 1.4 m/s in the radial direction of the membrane. At 800 rpm, the variation trends and trajectories of tangential velocity on the membrane with the transmembrane pressure of 0.5 bar, 1 bar, 1.5 bar, and 2 bar were similar. The tangential velocity on the membrane surface gradually increased to 4 m/s in the radial direction of the membrane, which was 3 times the tangential velocity at 300 rpm.
Fig. 8. Cloud diagram of shearing velocity on the membrane surface at 300 rpm: a = 0.5 bar, b = 1 bar, c = 1.5 bar, and d = 2 bar.
Units: m/s

8.79e+00
5.61e+00
4.43e+00
3.25e+00
2.07e+00
8.93e-01
-2.86e-01
-1.47e+00
-2.65e+00
-3.82e+00
-5.00e+00

Units: m/s

8.56e+00
6.92e+00
5.28e+00
3.65e+00
2.01e+00
3.72e-01
1.27e+00
2.90e+00
4.54e+00
6.18e+00
7.81e+00
**Fig. 9.** Cloud diagram of shearing velocity on the membrane surface at 800 rpm: a = 0.5 bar, b = 1 bar, c = 1.5 bar, and d = 2 bar.

**Fig. 10.** The tangential velocity on the membrane surface at 300 rpm variation with the radius of the filter membrane.
Fig. 11. The tangential velocity on the membrane surface at 800 rpm variation with the radius of the filter membrane

Fig. 12. Tangential flow velocity regression line on membrane surface at 300 rpm and 800 rpm
By comparing the cloud diagram of tangential velocity on the membrane surface in Figure 8 and 9, it can be seen that the tangential velocity at 800 rpm was significantly higher than that at 300 rpm. According to formula 3, it can be concluded that at 800 rpm, the shearing force generated by the blades on the membrane surface was higher than that at 300 rpm. That is, compared with 300 rpm, the filtered flux of black liquid was higher at 800 rpm. According to the experiment results of average filtered flux in Fig. 3, the filtered flux at 800 rpm was slightly higher than that at 300 rpm, with slight differences. The change curve of tangential flow velocity in Figs. 10 and 11 was linearly regressed, and a tangential flow velocity regression line on the membrane surface at 300 and 800 rpm was obtained. The relationship between the membrane radius and the tangential flow velocity were thus obtained. The tangential flow velocity on any position on the membrane surface can be calculated by the trend line in Fig. 12.

**Blade Pressure Variation**

The rotating blade in the dynamic cross-flow filtration chamber conducts shearing action on the black liquor, which causes the black liquor to exert pressure on the rotating blades. The pressure variations are shown in Figs. 13 and 14. Because the pressure variation is caused by the pressure of the black liquor on the blade due to the blade rotation, this paper presents the variation trend of dynamic pressure with blade radius as shown in Figs. 15 and 16. The dynamic pressure of the blade increased with the radius and reached the maximum at the outer edge of the blade. At 300 rpm and when the membrane pressure was 1 bar, the maximum dynamic pressure reached 1300 Pa; at 300 rpm and when the membrane pressure was 2 bar, and the minimum value of maximum dynamic pressure was 1100 Pa. At 800 rpm and when the transmembrane pressure was 0.5 bar, 1 bar, 1.5 bar, and 2 bar, the variation trajectories and trends of blade pressure were similar. The maximum dynamic pressure was approximately 9000 Pa, which was 7 times the maximum pressure on the blade at 300 rpm. According to Figs. 13 through 16, it can be seen that the rpm had an effect on the pressure of the blade, while the transmembrane pressure difference had little effect on the pressure of the blade.

**Comparison of Flux Results**

According to the experimental and simulation results of capturing pulping black liquor by the blade cross-flow nanofiltration membrane, the average filtered flux of black liquor is the most ideal when the transmembrane pressure is 0.5 bar, as shown in Fig. 17. The flux change is basically the same as the experiment obtained in the simulation, and the comparison result verifies the simulation model of blade dynamic cross-flow, which shows that the simulation model is accurate.

According to the simulation results of the pressure on the blades, the pressure on the blades at 800 rpm is 7 times that at 300 rpm. According to the simulation results of the tangential flow velocity of the membrane surface, the tangential flow velocity of the blades at 800 rpm is 3 times that at 300 rpm. It can be seen from Fig. 17 that the filtered flux of black liquid was not much different between 300 rpm and 800 rpm. According to the above experiments and simulation results, when the blade dynamic cross-flow uses 1kDa nanofiltration membrane to filter black liquor, the average filtered flux of black liquor was not much different between 800 rpm and 300 rpm. The filtration process at 800 rpm consumes more energy, and the blade is under more pressure, thus shortening the service life.
Fig. 13. Cloud diagram of blade pressure change at 300 rpm: a = 0.5 bar, b = 1 bar, c = 1.5 bar, and d = 2 bar
**Fig. 14.** Cloud diagram of blade pressure variation at 800 rpm: a = 0.5 bar, b = 1 bar, c = 1.5 bar, and d = 2 bar.

Fig. 15. Variation of blade dynamic pressure with radius at 300 rpm

Fig. 16. Variation trend of blade dynamic pressure with radius at 800 rpm
CONCLUSIONS

With the blade dynamic cross-flow filtration equipment, and three membranes with different capturing size of molecule, the flux experiment of pulping black liquor was conducted, and the lignin content in the black liquor by the nanofiltration membrane NP010 was high. In this regard, the paper used CFD software Fluent to simulate the filtration of paper-making black liquor by the blade cross-flow nanofiltration membrane. The results of black fluid flux were obtained respectively by comparing the experiment and simulation, and the tangential velocity and blade stress on the blade cross-flow nanofiltration membrane surface were examined during the filtration process. The main conclusions are as follows:

1. The simulated flux results were similar to the experimental results. At 300 rpm or 800 rpm, the flux of black liquor was optimal at a transmembrane pressure of 0.5 bar. According to the experimental and simulation results, it can be seen that the blade dynamic cross-flow uses 1 kDa nanofiltration membrane to filter the black liquor at 300 rpm, and the average flux at 800 rpm is about the same, but it consumes less energy and the pressure is less on the blade.

2. At 300 rpm and 800 rpm, the maximum shear velocity on the membrane was 1.4 m/s and 4 m/s, respectively, which was located at $R = 64$ mm, that is, the blade edge. The tangential velocity on the membrane surface at 800 rpm was three times that of 300 rpm, so the corresponding shearing stress on the membrane was also three times.

3. From the blade pressure variation in Figs. 13 and 14, it can be seen that at 800 rpm, the maximum pressure on the blade was 7 times that of 300 rpm.
ACKNOWLEDGMENTS

The authors give sincere gratitude to Professor Wu Junfei and Professor Chen Fushan from Qingdao University of Science and Technology, Professor Hermann Nirschl and a fellow colleague Herr Zihim Lam from the Institute of Mechanische Verfahrenstechnik und Mechanik (MVM), which is affiliated to Institute of Karlsruhe Technology (KIT) for their academic assistance and help, also extend thanks to the Fund Project (2019GHY112040) for their support on finance.

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Article submitted: January 27, 2020; Peer review completed: April 25, 2020; Revised version received and accepted: Mary 21, 2020; Published: May 29, 2020. DOI: 10.15376/biores.15.3.5593-5615