

Theoretical Determination of Pit Membrane Natural Frequency for Destruction by Resonance Effect

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The low permeability of many wood species causes significant problems during processing. Industrial methods used for increasing wood permeability reduce strength properties, are energy consuming, and are not viable economically. Destruction of pit membranes in wood cell walls can provide an increase in wood permeability without affecting wood strength properties. It can be accomplished using resonance applied to the pit membranes. Theoretical analysis and calculations have been performed to determine pit membrane (torus and margo) natural frequency. Membrane natural frequencies of bordered pits of Norway spruce are in the range of 3 to 11 MHz. Water in the pit chamber did not have a significant effect on the resonant frequency of the membrane. The main limitation of the amplitude of membrane fluctuations inside the pit chamber was the width of the chamber. Two methods to initiate resonance frequency for pit membrane destruction have been suggested, namely, alternating electric field application and microwave energy pulsation.

Keywords: Bordered pits; Margo; Microwave treatment; Resonance frequency; Torus; Wood permeability

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INTRODUCTION

Many wood species have low permeability, which can cause problems during the processing of the wood material. Examples of problems are penetration of chemicals during processing of chemical pulp, long and expensive drying times, material loss after timber drying, and difficulties of timber impregnation with preservatives. Therefore, it is essential for the pulp- and timber industry to find new methods that can provide an increase of wood permeability without negative effects on the morphology and strength properties of wood.

Some methods for increasing wood permeability such as steam explosion (Mason 1926) and microwave (MW) wood modification (Torgovnikov and Vinden 2009) have been tested. Intensive MW power applied to wood generates steam pressure within wood cells. Under high internal pressure, pit membranes in wood cell walls and tyloses in vessels and ray parenchyma cells rupture to form pathways for easy transportation of liquids and vapor into the wood. However, the method has significant shortcomings, *e.g.*, reduction of wood strength properties, high-energy consumption, and microwave equipment cost. In comparison, steam explosion increases wood permeability but ruptures the entire wood structure, thereby significantly reducing strength properties along with high-energy consumption. Therefore, these methods have limited applications in industry, particularly in solid wood processing.

An interesting technological question is whether tracheid pit membranes in softwoods can be ruptured selectively to allow a significant increase in wood permeability

without destruction of other wood structural elements, *i.e.*, without negative effects on the wood physical and mechanical properties. The range of pit membrane (torus and margo) natural oscillation frequencies can be calculated, making possible the application of resonance forces to destroy pit membranes. The aim of the present theoretical study is to determine the range of pit membrane natural oscillation frequencies of softwoods. As an example, the study focuses on Norway spruce (*Picea abies* (L.) Karst.) that has low permeability but is highly used in the pulp and paper and saw mill industries. Table 1 contains abbreviations used in this paper.

Table 1. Symbols and Abbreviations

Symbol	Definition	Unit
A_c	Maximum amplitude of membrane vibration	μm
c_s	Sound velocity	cm/s
D	Diameter of margo	μm
d	Diameter of torus	μm
d_a	Aperture diameter	μm
E	Young's modulus	dyn/cm^2
F_c	Force of resistance to movement in water	dyn
F_e	Elastic force per unit length	dyn/cm
F_i	Inertial force per unit length	dyn/cm
F_p	Breaking force	dyn
f	Frequency	Hz
f_0	Resonance frequency	Hz
H	Torus thickness	μm
H_c	Chamber width	μm
h	Margo thickness	μm
h_c	In the model: Margo thickness	μm
h_m	In the model: Membrane thickness	μm
I	Moment of inertia of the cross section of membrane	m^4
k	Wave vector	cm^{-1}
i	Imaginary part	
r	Radius	μm
S	Membrane cross-sectional area in perpendicular plane	μm^2
S_c	Pit chamber cross-sectional area	μm^2
S_o	Area of the sum of openings in margo and aperture	μm^2
$\partial = S_c/S_o$	Ratio of the area of the passage of the pit chamber to the sum of the area of the passage in margo and aperture	
V	Velocity	cm/s
zV_1	Average membrane velocity	cm/s
z	Coordinate axis	
γ	Excitation frequency	Hz
ε	Relative elongation (tensile deformation)	μm
η	Dynamic viscosity	g/cm s
λ	Wavelength	nm
ν	Kinematic viscosity	cm^2/s
ρ	Cellulose density	g/cm^3
ρ_w	Water density	g/cm^3
σ_t	Tensile strength	dyn/cm^2
$\omega = 2\pi f$	Angular (circular) frequency	rad/sec
ω_0	Imaginary frequency	Hz

EXPERIMENTAL

Frequency Calculation of Pit Membrane Resonance

Many publications have discussed the morphology and functions of simple, bordered (Fig. 1), and half-bordered pits in conifers.

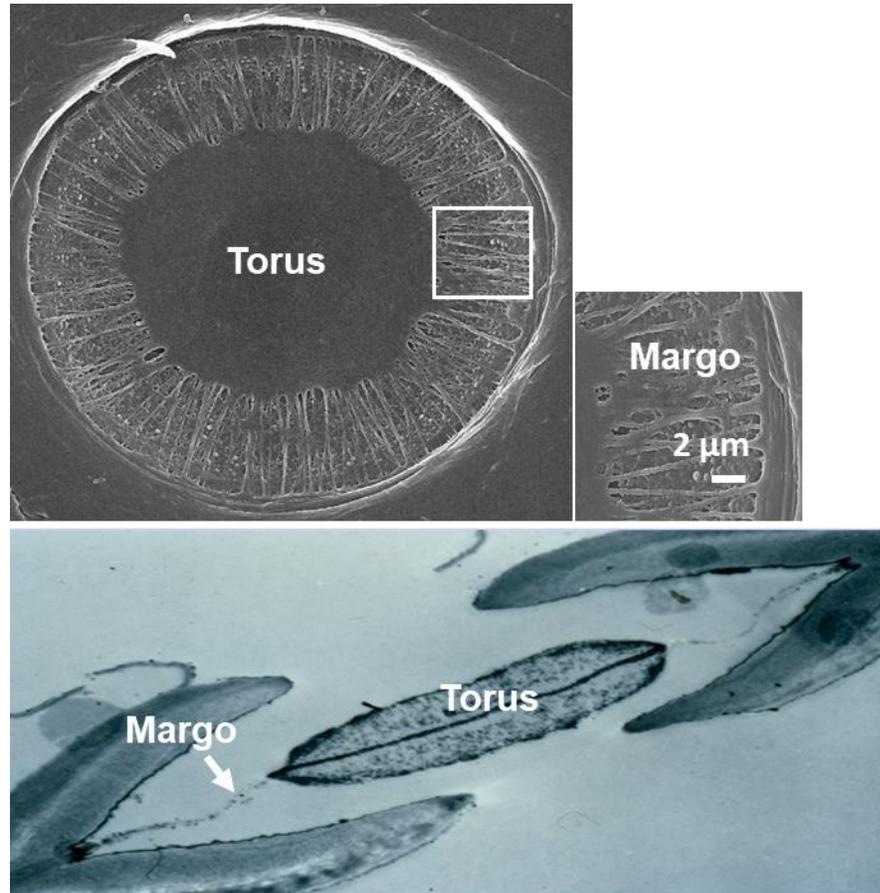


Fig. 1. Scanning and transmission electron micrographs of aspirated (above) and unaspirated bordered pit (underneath)

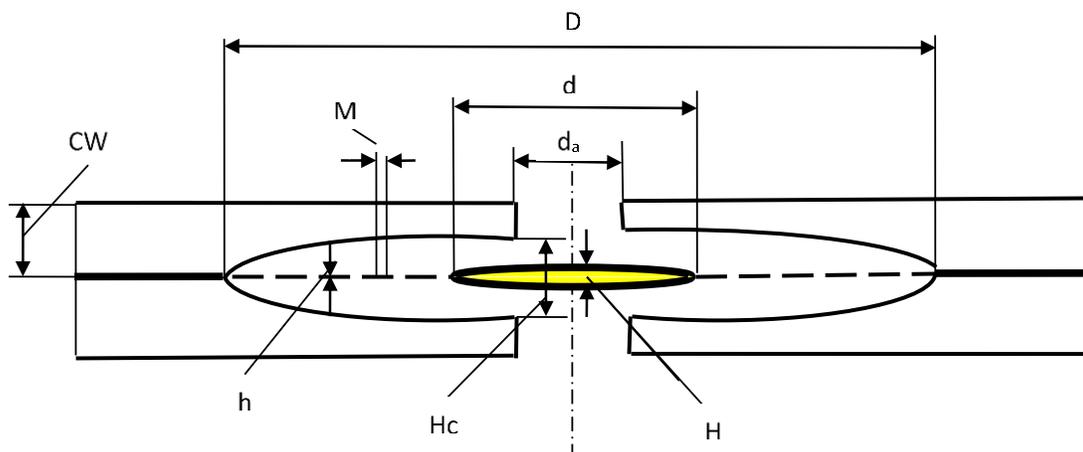


Fig. 2. Specific dimensions of a bordered pit described further in Table 2

Table 2. Data on Bordered Pit Dimensions (μm) of Norway Spruce. Cell Wall Substance Density - 1.53 g/cm^3 , Density of Cellulose - 1.55 g/cm^3

	Minimum	Maximum	Average
Cell wall thickness CW			
Earlywood	2.8	3.5	3.2
Latewood	3.2	5.0	4.1
Pit chamber diameter D			
Earlywood	10	25	17.5
Latewood	10	15	12.5
Pit chamber aperture d_a			
Earlywood	1.4	5.0	3.2
Latewood	1.4	5.0	3.2
Pit chamber width H_c in earlywood is adopted as cell wall thickness $\times 2$; for latewood it is equal to the cell wall thickness			
Earlywood	$2.8 \times 2 = 5.6$	$3.5 \times 2 = 7.0$	6.3
Latewood	3.2	5.0	4.1
Torus diameter d (twice as large as aperture diameter d_a ; (Siau, 1984), <i>i.e.</i> $d = 2d_a$)			
Earlywood	2.8	10	6.4
Latewood	2.8	10	6.4
Torus thickness H			
Earlywood	0.2	1.0	0.6
Latewood	0.3	1.2	0.75
Margo diameter D			
Earlywood	10	25	17.5
Latewood	10	15	12.5
Margo thickness h			
Earlywood	0.1	0.5	0.2
Latewood	0.1	0.5	0.2
Openings in margo, M			
Early wood			0.25
Late wood			0.25

Saren *et al.* (2001), Zimmermann (1983), Siau (1984), Stamm (1964), Brändström (2001), Rosner *et al.* (2007), and Mayr *et al.* (2003) are the most relevant when describing the dimensions of Norway spruce bordered pits; the above literature findings have been compiled in Table 2 and illustrated in Fig. 2.

Pit Membrane Model

By definition, the torus is a continuous medium and presented as a cylinder with diameter d and thickness H (Fig. 3). For simplification, it is presumed that the microfibrillar strands of the margo are also a continuous medium.

Because the microfibrillar strands of the margo are thinner than the torus, they are expressed as one thinner cylinder with external and internal diameters D and d and a thickness $h_c(r)$, which decreases along the radius (Fig. 3). Thickness decrease is justified by the fact that the constant number of strands originating from the torus reach the periphery of the pit chamber with larger diameter than torus. Thus, the relationship between $h_c(r)$ and the radius $D/2$ is presumed linear.

$$h_c(r) = h \left(1 - \frac{2 \left(r - \frac{d}{2} \right)}{D} \right) \quad (1)$$

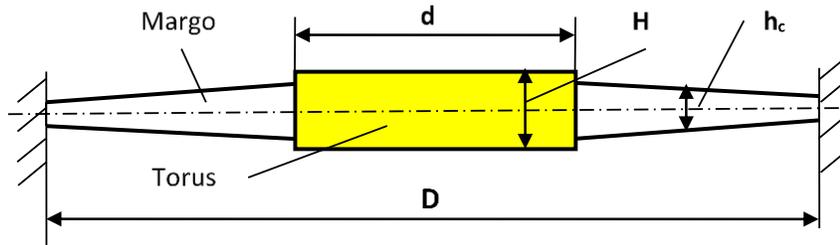


Fig. 3. Model of a pit membrane consisting of torus and margo

The model of torus and margo (called *membrane*), consists of 2 cylinders forming one entity with a thickness $h_m = H$ when $r < \frac{d}{2}$ or $h_m = h_c(r)$ when $\frac{d}{2} < r < \frac{D}{2}$. It should be noted that the sharp change in the thickness of the membrane at the junction of the two cylinders will affect the shape of the membrane when deflected, *i.e.*, it will be distorted. A tangent to the midline of the membrane will experience a jump at the junction when moving from one cylinder to another. Practically the jump will not affect the frequency of natural oscillations, as a system with a continuous mass distribution is not sensitive to local perturbations.

For quantitative calculations of membrane fluctuation characteristics caused by bending, the moment of inertia of the membrane related to its midline (dashed line in Fig. 3) and the area of this section are required. The moment of inertia of the membrane cross section in the plane of Fig. 3 related to its midline, by the definition of Landau and Lifshitz (1986), is shown in Eq. 2.

$$I = \int_{-d/2}^{d/2} dr \int_{-H/2}^{H/2} z^2 dz + 2 \int_{d/2}^{D/2} dr \int_{-h(1-2(r-\frac{d}{2}))/2}^{h(1-2(r-\frac{d}{2}))/2} z^2 dz \quad (2)$$

The first integral is the moment of inertia of torus (inner cylinder) and the second integral the moment of inertia of margo (outer cylinder), which are shown within the limits of integration. Computing the integrals results in Eq. 3.

$$I = \frac{H^3 d}{12} + h^3 D \left(1 + \left(\frac{d}{D}\right)^4\right) / 48 \quad (3)$$

The value $\left(\frac{d}{D}\right)^4 \approx \frac{1}{50}$, *i.e.* it is negligible; thus, the moment of inertia is given in Eq. 4.

$$I = \frac{H^3 d}{12} + \frac{h^3 D}{48} \quad (4)$$

The membrane cross-sectional area is the sum of the area of torus (the rectangle $H \times d$), and the area of the isosceles trapezoid where the two legs are of equal length and described by formula (1). The area is calculated as shown in Eq. 5.

$$S = Hd + h \left(1 + \frac{d}{D}\right) (D - d) / 2 \quad (5)$$

Thus, the preparatory operations are completed. For a better understanding of the degree of influence of various factors on the frequency of natural fluctuations of membrane, three examples are considered.

Membrane Fluctuations in Air

Neglecting the presence of pit chamber and water and presume that the membrane is in air. An equation describing the vibrations of the membrane can be derived (Fig. 4).

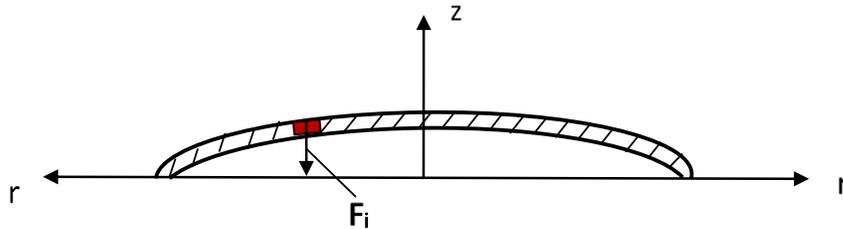


Fig. 4. Membrane model for calculations

When the membrane is deflected, the inertial force F_i per unit of its length is given by Eq. 6,

$$F_i = -\rho S z_t'' \quad (6)$$

where z_t'' is the partial derivative of 2^d order with regard to time. The elastic force caused by the deflection of the membrane per unit length is determined by the formula of Landau and Lifshitz (1986) (Eq. 7),

$$F_e = E(I z_r'')'' \quad (7)$$

where z_r'' is the partial derivative with regard to the 2^d order radial coordinate and E is the Young's modulus. Taking the derivative of $(I z_r'')$ results in Eq. 8,

$$F_e = EI'' z_r'' + EI z_r'''' \quad (8)$$

where z_r'''' is the partial derivative with regard to the 4th order radial coordinate. For the moment of inertia in Eq. 4, the first term on the right-hand side is zero, as I is a constant.

Equating the inertial and elastic forces (Eq. 6) and (Eq. 8) to each other, a 4th degree partial differential equation is obtained.

$$EI z_r'''' + \rho S z_t'' = 0 \quad (9)$$

Substituting the moment of inertia of section (Eq. 4), sectional area (Eq. 5) in (Eq. 9) and reducing it by Hd , Eq. 10 is obtained.

$$\frac{EH^2 \left(1 + \frac{h^3 D}{4H^3 d}\right)}{12\rho z_r''''} + \left(1 + \frac{\left(\frac{D}{d} - \frac{d}{D}\right)h}{2H}\right) z_t'' = 0 \quad (10)$$

To find the vibration frequency in Eq. 10, its dispersion equation should be used to find the relationship $\omega = f(k)$. Thus, Eq. 10 was substituted in the form of a wave perturbation $z = z_0 \exp(-i(\omega t - kr))$, whose partial derivatives are:

$$z_t'' = -z_0 \omega^2 \exp(-i(\omega t - kr)) \text{ and } z_r'''' = z_0 k^4 \exp(-i(\omega t - kr)) \quad (11)$$

Substituting the derivatives (Eq. 11) into Eq. 10, $\omega = f(k)$ is obtained.

$$\omega = \left(\sqrt{Hk^2 \left(\frac{E}{12\rho}\right)}\right) \sqrt{\left(\left(1 + \frac{h^3 D}{4H^3 d}\right) / \left(1 + \left(\frac{D}{d} - \frac{d}{D}\right)h / 2H\right)\right)} \quad (12)$$

Equation 12 is a form that is convenient for analysis. It is desirable to apply low frequencies or long wavelengths for an effective impact on the membrane to rupture it. The entire system should be effected; the membrane takes the form of half the period of a sinusoid during deflection as shown in Fig. 4. The lowest frequency is obtained when half the wavelength λ is in the system, *i.e.* $\lambda = 2D$ or $k = \pi/D$, which corresponds to the main resonance. Having completed these procedures, the main resonant frequency was obtained in Eq. 13,

$$f_0 = \pi A H c_s / 4D^2 \sqrt{3} \quad (13)$$

where:

$$A = \sqrt{\left(1 + \frac{h^3 D}{4H^3 d}\right) / \left(1 + \frac{\left(\frac{D}{d} - \frac{d}{D}\right) h}{2H}\right)}$$

The main resonant frequencies for the data in Table 2 and velocity $c_s = 4.9 \times 10^5$ cm/s, calculated by assuming $E = 3.7 \times 10^3$ kg/mm² = 3.7×10^{11} dyn/cm² and $\rho = 1.55$ g/cm³ (Sjöström 1993) are presented in Table 3. The speed of sound in a solid body with a small Poisson's ratio is $c_s = \sqrt{\frac{E}{\rho}}$ (Landau and Lifshitz 1986).

Table 3. Destructive Resonant Frequencies for Early- and Latewood Membranes

	Resonant Frequency (MHz)	
	Earlywood	Latewood
Minimum-size Membranes	3.45	5.4
Average-size Membranes	3.4	8.9
Maximum-size Membranes	2.8	10.9

Analysis of the resonant frequencies shows that they are always larger in latewood due to an increase in membrane stiffness. Latewood torus has greater thickness (0.3 μm versus 0.2 μm in earlywood, Table 2). The stiffness is higher, and it is more difficult to bend, which explains the minimum values. For the maximum values, latewood has a membrane diameter of 15 μm , while earlywood has 25 μm (Table 2). The membrane is shorter, the stiffness is higher, and, as above, it is more difficult to bend. The multidirectional change in the main resonance frequency of the early- and latewood pit membranes in the transition from minimum to maximum values is also interesting: in earlywood, the frequency decreases, while in latewood it increases. This is because the ratio of the maximum and minimum diameters of the margo in earlywood is 2.5, but only 1.5 in latewood; the ratio of the maximum and minimum torus thickness in the early- and latewood is 5 and 4 respectively (see Table 2). Therefore, the frequency in the earlywood changes as $5/2.5^2$, *i.e.* 0.8 times < 1 , and in the latewood $4/1.5^2 = 1.78$ times > 1 .

Membrane Fluctuations in Water

The effect of water on membrane fluctuations is considered, disregarding the pit chamber. During fluctuations in water, a viscosity force will act on the membrane, inhibiting its movement. The viscosity force should be introduced in Eq. 9. The formula of the viscosity force depends on the regime of body motion in the fluid, which is determined by Reynolds number; $Re = \frac{\rho a V}{\eta} = aV/\nu$, where a is a characteristic dimension.

In this case, the characteristic dimension is $a = d$, because, as shown in the next section, water flows through the margo quite freely and the main resistance is caused by the torus. The membrane velocity estimate is obtained from analysis of membrane vibrations found in the previous section.

During the oscillation period $1/f_0 \approx 0.3 \mu\text{s}$, the membrane passes a distance equal to two-chamber widths $\approx 10 \mu\text{m}$ (in one period, *i.e.*, forward and back); therefore, its average speed is $V_1 \approx 3000 \text{ cm/s}$. The dynamic viscosity of water is $\eta = 10^{-2} \text{ g/cm s}$. Substituting all values produces $Re = d\rho V_1/\eta \approx 100$. Thus, despite the high speed, the Reynolds number is small since the dimensions of the “moving object” are very small ≈ 3 to $5 \mu\text{m}$. The small Reynolds number shows that the flow regime is practically laminar and the relationship of the viscosity force and the velocity is linear; thus, the force formula is $F_c \approx 40\eta dV$ (Ebert 1976). By introducing the force per unit length of the membrane, equal to the force $F_c \approx 40\eta dV$ and by dividing by the membrane diameter D and considering $V = z_t'$ in Eq. 9 as the force per unit length of the membrane $\frac{F}{D}$, Eq. 14 is obtained.

$$EIz_r'''' + 40\eta\left(\frac{d}{D}\right)z_t' + \rho S z_t'' = 0 \quad (14)$$

Transforming Eq. 14 further produces Eq. 15.

$$EI + 40vd/DSz_t' + z_t'' = 0 \quad (15)$$

Transition to the dispersion equation is done in the same way as in the previous section (as in Eq. 11). After substituting $z = z_0 \exp(-i(\omega t - kr))$, a new dispersion equation is obtained.

$$\frac{EI}{\rho S k^4} - \frac{i40vd}{(DS\omega - \omega^2)} = 0 \quad (16)$$

Due to the existence of an imaginary quantity in Eq. 16, the frequency solution in the form $\omega = \omega_0 + i\gamma$ is required, where ω_0 is the real part of the frequency and γ is the imaginary term presenting the attenuation. Substituting ω into Eq. 16,

$$\omega_0 = \sqrt{\left(\frac{EI}{\rho S}\right)k^4 - 400((vd)^2/(DS)^2)} \quad (17)$$

$$\gamma = -20vd/DS$$

The first term under the root in Eq. 17 is the frequency defined by Eqs. 12 and 13. The second term is a newly added item, considering the viscosity that leads to a decrease in frequency. Evaluating its effect on the frequency found in the previous section, and considering that $k = \pi/D$ and $\pi^2 \approx 10$, the ratio of the additive to the frequency is shown below.

$$4dD^3v^2/ISc_s^2 \quad (18)$$

An example is the calculations of the characteristics of the most “influential” case: earlywood with minimum dimensions $D = 10 \mu\text{m}$, $H = 0.2 \mu\text{m}$, $h = 0.1 \mu\text{m}$, $d = 2.8 \mu\text{m}$ (Table 2), $v = 10^{-2} \text{ cm}^2/\text{s}$, $c_s = 4.9 \times 10^5 \text{ cm/s}$ that are substituted in Eqs. 4 and 5, and then I and S are calculated, and finally calculating Eq. 18, the result is approximately 0.01. This is the worst case; when other values from Table 2 are substituted, the correction is even less. This small supplement does not affect the results. This demonstrates that the effect of water on the fluctuation frequency is negligible and, therefore, it can be determined by Eq.

13.

Membrane Fluctuations in a Pit Chamber Filled With Water

When the membrane oscillates in water, water will flow through the membrane during its movement without any obstacle. In a pit chamber, when the membrane fluctuates from the equilibrium position, water due to its incompressibility, is forced to flow from the chamber through the pit aperture, to which the membrane moves, and flow from the other side of the membrane through the openings in the margo (Fig. 5).

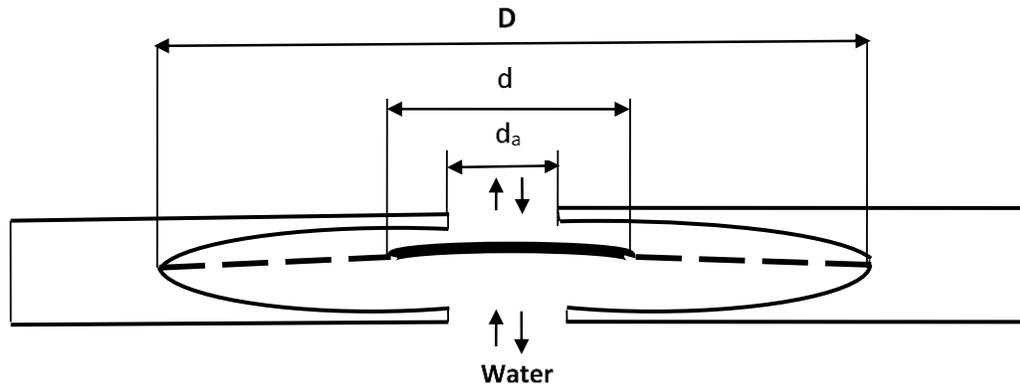


Fig. 5. Water movement through a pit membrane during fluctuation

When pumping water through both openings (*i.e.*, pit aperture and margo), a differential pressure will occur relative to the two sides of the membrane, which will inhibit its movement. Comparing the free space in margo and pit apertures, the aperture area is $\pi d_a^2/4$. The opening area in a real margo (assuming 80 strands), is determined by the difference in the margo area minus the area of the strands and is equal to $\frac{\pi(D^2-d^2)}{4} - 80h(D-d)/2$. Substituting the data, the area of the openings in the margo exceeds the area of the aperture by 5 to 28 times depending on the parameters of the pit, and thus, the main flow of water will pass through the margo. The water velocity in the pit chamber V_1 is equal to the instantaneous membrane velocity z_t' multiplied by the ratio of the torus area to the membrane area, which is $\delta = (\frac{d}{D})^2$, *i.e.* $V_1 = \delta z_t'$. A simplified assumption is that the entire membrane moves like a piston, where the torus pumps the water in contrast to the margo.

To find the resistance force of water flowing through the margo, we simulate its strands as cylinders with a diameter h . In this case, the Reynolds number is $Re \approx \frac{h\rho_w V_1}{\eta} = 10$. For such a flow, the resistance force of one cylinder of length $\frac{D-d}{2}$ according to Ebert (1976) is shown below.

$$F_c = 10\eta(D-d)\delta z_t' \quad (19)$$

The thickness of margo strands is not in the formula. It is indirectly included in the coefficient, depending on the Reynolds number, for all 80 strands.

$$F_c = 80 \times 10\eta(D-d)\delta z_t' \quad (20)$$

Substituting the force (Eq. 20) referred to the diameter of the membrane into Eq. 9 produces Eq. 21 or 22.

$$EIz_r'''' + 400 \left(1 - \frac{d}{D}\right) \eta \delta z_t' + \rho S z_t'' = 0 \quad (21)$$

$$\left(\frac{EI}{\rho S}\right) z_r'''' + \frac{400 \left(1 - \frac{d}{D}\right) \eta \delta z_t'}{\rho S} + z_t'' = 0 \quad (22)$$

Substituting the values of the derivatives z from Eq. 11,

$$\frac{EI k^4}{\rho S} - \frac{i 400 \left(1 - \frac{d}{D}\right) \eta \delta \omega}{\rho S} - \omega^2 = 0 \quad (23)$$

Solving Eq. 23,

$$\omega_0 = \sqrt{\left(\frac{EI}{\rho S}\right) k^4 - (200 \eta \left(1 - \frac{d}{D}\right) \delta / \rho S)^2} \quad (24)$$

$$\gamma = -200 \eta \left(1 - \frac{d}{D}\right) \delta / \rho S$$

Recalling that $\omega = 2\pi f$, and without the last term in Eq. 24, Eq. 24 determines the oscillation frequency of a free membrane; see Eqs. 12 and 13. Accordingly, Eq. 24 is transformed, introducing f_c - the oscillation frequency of the membrane in the chamber.

$$f_c = \sqrt{f_0^2 - (100 \eta \left(1 - \frac{d}{D}\right) d^2 / \pi \rho D^2 S)^2} \quad (25)$$

The ratios of membrane frequencies in the pit chamber calculated by Eq. 25 to the frequencies in free water f_c/f_0 are given in Table 4.

Table 4. Ratios of Membrane Frequencies in Pit Chambers

	Minimum dimensions of pit	Maximum dimensions of pit	Average dimensions of pit
Earlywood	0.94	0.99	0.98
Latewood	0.99	0.96	0.99

In earlywood, the decrease of frequency in the region of minimum size is due to the small thickness of the torus or the small mass making the membrane less inertial. In latewood, the decrease of frequency in the region of maximum sizes is due to the relative decrease in the size of margo, which complicates the flow of water through it. However, the effect of the pit chamber on the resonant frequency in all cases is not significant.

The influence of the pit chamber on fluctuations can have another effect, namely, to limit the fluctuation amplitude. The membrane should deviate to a distance sufficient to tear the margo strands, and the chamber walls should not interfere with this deviation, *i.e.*, the oscillation amplitude of the membrane at which the strands will rupture must satisfy the condition $A_c < \frac{1}{2} H_c$. The maximum amplitude is apparently equal to the maximum deviation of the membrane, at which the strands tear due to their elongation. The maximum allowable elongation (Ebert 1976) is $\varepsilon \approx \frac{\sigma_t}{E} \approx 7 \times 10^8 / 3.7 \times 10^{11} \approx 0.002$; consequently $A_c = 0.1D$ is calculated. Thus, the margo can be destroyed by the resonance frequency of the membrane for which the condition $0.1D < \frac{1}{2} H_c$ or $\frac{D}{H_c} < 5$ is fulfilled.

The necessary requirement $\frac{D}{H_c} < 5$ is fulfilled for all cases, but considering the large spread in the strength limits of cellulose (Sjöström 1993; Monteiro *et al.* 2011), a problem

can arise when trying to destroy margo strands of maximum sizes, especially in earlywood spruce tracheids.

RESULTS AND DISCUSSION

Theoretical calculations and their analysis showed the main resonant frequencies of bordered pit membranes for Norway spruce wood in the range of 3 to 11 MHz. The accuracy of the calculation results are determined by the accuracy of the physical characteristics of the torus and margo. Water filling the pit chamber does not have a significant effect on the main resonant frequencies of the membrane; with increasing temperature, this effect decreases even more due to a decrease in the water viscosity. The effect of pit apertures restricting the flow of water during the movement of the membrane does not affect the vibrations of the membrane inside the pit chamber due to the permeability of the margo to water.

The main limitation of the amplitude of membrane fluctuations inside the pit chamber can be the width of the chamber. To eliminate the effect of the membrane touching the walls of the chamber, it is possible to irradiate the membrane with twice the main resonant frequency. In this case, the shape of the membrane during deviations will be sinusoidal with zero deviation in the middle of the chamber, and not semi-sinusoidal with a maximum deviation in the middle of the chamber.

In order to initiate pit membrane resonance oscillations it is necessary to apply forces acting in opposite directions with a required frequency. Two possible methods are discussed. Water in wood contains ions with various mobility. In an electric field, the membrane will be charged by mobile ions and can move under alternating electric field in opposite directions. Alternating electric field applied perpendicular to membrane will initiate mechanical forces to move the membrane and destroy the margo. An ideal frequency for rupturing is the resonance frequency of the pit membranes (*i.e.*, 3 to 11 MHz). The desired range of frequencies of electromagnetic radiation can be achieved using a klystron.

Another method of pit membrane fluctuation is creating a pressure in the wood cell and transmitting the pressure to adjacent cells with a frequency within the membrane natural frequency range. To cause membrane oscillation, it is necessary to apply pressure alternatively from both sides of the pit membrane. Alternation of pressure application with required frequency can possibly be achieved by applying MW power for water evaporation in tracheids from alternate sides of the membrane. For example, a MW generator working at a frequency of 2.45 GHz will emit enough energy for sufficient boiling of water in the cell lumen during a short period. Steam in the tracheid applies pressure to the membrane causing it to deflect to one side. After the energy comes to the next tracheid, the steam in the cell creates a pressure and deflects the membrane in reverse direction. In this way, the membrane activates into oscillation mode. As the next portion of energy comes in a defined time, it will repeat the membrane oscillation. Repetition of the oscillations with a defined frequency will destroy the membrane and open the pit. Microwaves can bring into wood the required membrane vibrations. Pulse energy application with define range of pulsation frequency can possibly provoke the process of membrane rupturing which leads to an increase of wood permeability without reduction in strength properties.

CONCLUSIONS

1. The resonant frequencies of the membrane (torus and margo) of bordered pits of the sapwood of Norway spruce (and most likely other coniferous species) is found in the range of 3 to 11 MHz.
2. Water in the pit chamber does not have a noticeable effect on the resonant frequencies of the membrane. Margo is permeable for water and its influence on the water flow is low.
3. The main limitation of the amplitude of membrane fluctuations inside the pit chamber is the width of the chamber. The conclusion requires experimental confirmation.
4. Resonance frequency used for pit membrane disruption possibly requires less energy compared to other methods of increasing wood permeability. Pit membrane rupture would possibly not affect the wood mechanical properties.
5. Two methods for resonance frequency application for pit membrane destruction have been suggested, namely alternating electric field application and microwave energy pulsation.

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